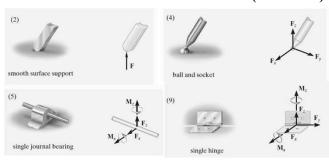


change in forces, failure might occur.

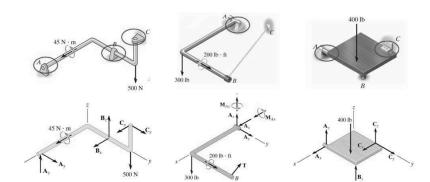
SUPPORT REACTIONS IN 3-D (Table 5-2)



A few examples are shown above. Other support reactions are given in your text book (Table 5-2).

As a general rule, if a <u>support prevents translation</u> of a body in a given direction, then a <u>reaction force</u> acting in the opposite direction is developed on the body. Similarly, if <u>rotation is prevented</u>, a <u>couple moment</u> is exerted on the body by the support.

IMPORTANT NOTE



A single bearing or hinge can prevent rotation by providing a resistive couple moment. However, it is usually preferred to use two or more properly aligned bearings or hinges. Thus, in these cases, only force reactions are generated and there are no moment reactions created.

EQUATIONS OF EQUILIBRIUM

(Section 5.6)

As stated earlier, when a body is in equilibrium, the net force and the net moment equal zero, i.e., $\Sigma F = 0$ and $\Sigma M_0 = 0$.

These two vector equations can be written as <u>six scalar</u> equations of equilibrium (EofE). These are

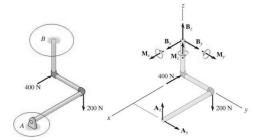
$$\Sigma F_X = \Sigma F_Y = \Sigma F_Z = 0$$

$$\Sigma M_X = \Sigma M_Y = \Sigma M_Z = 0$$

The moment equations can be determined about any point.

Usually, choosing the point where the maximum number of unknown forces are present simplifies the solution. Any forces occurring at the point where moments are taken do not appear in the moment equation since they pass through the point.

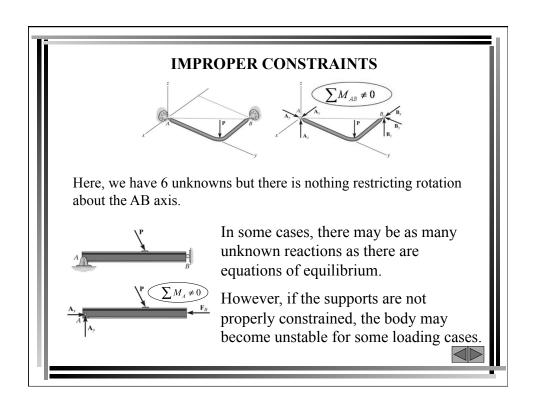
CONSTRAINTS AND STATICAL DETERMINACY (Section 5.7)



<u>Redundant Constraints</u>: When a body has more supports than necessary to hold it in equilibrium, it becomes statically indeterminate.

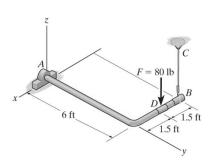
<u>A problem that is statically indeterminate</u> has more unknowns than equations of equilibrium.

Are statically indeterminate structures used in practice? Why or why not?



I	READING QUIZ
	If a support prevents rotation of a body about an axis, then the support exerts a on the body about that axis.
	A) Couple moment B) Force
	C) Both A and B. D) None of the above.
	When doing a 3-D problem analysis, you have scalar equations of equilibrium.
	A) 3 B) 4
	C) 5 D) 6

EXAMPLE



Given: The rod, supported by thrust bearing at A and cable BC, is subjected to

an 80 lb force.

Find: Reactions at the thrust

bearing A and cable BC.

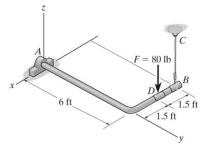
Plan:

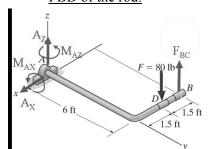
- a) Establish the x, y and z axes.
- b) Draw a FBD of the rod.
- c) Write the forces using scalar equations.
- d) Apply scalar equations of equilibrium to solve for the unknown forces.



EXAMPLE (continued)

FBD of the rod:





Applying scalar equations of equilibrium in appropriate order, we get

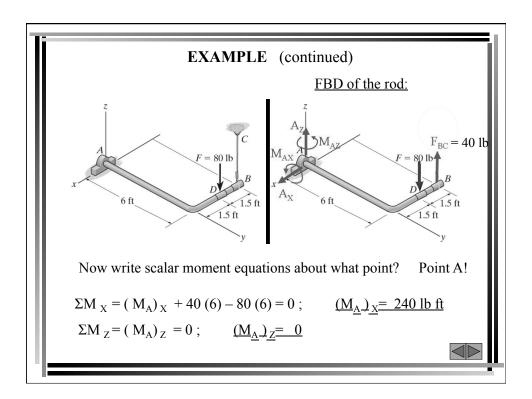
$$\Sigma F_X = A_X = 0$$
; $\underline{A_X} = 0$

$$\Sigma F_Z = A_Z + F_{BC} - 80 = 0$$
;

$$\Sigma M_{Y} = -80 (1.5) + F_{BC} (3.0) = 0;$$

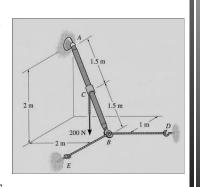
Solving these last two equations: $\underline{F}_{\underline{BC}} = 40 \text{ lb}$, $\underline{A}_{\underline{Z}} = 40 \text{ lb}$





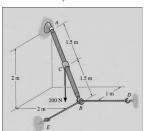
CONCEPT QUIZ

- 1. The rod AB is supported using two cables at B and a ball-and-socket joint at A. How many unknown support reactions exist in this problem?
 - A) 5 force and 1 moment reaction
 - B) 5 force reactions
 - C) 3 force and 3 moment reactions
 - D) 4 force and 2 moment reactions



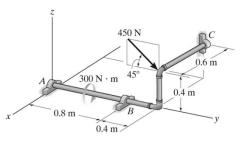
CONCEPT QUIZ (continued)

- 2. If an additional couple moment in the vertical direction is applied to rod AB at point C, then what will happen to the rod?
 - A) The rod remains in equilibrium as the cables provide the necessary support reactions.
 - B) The rod remains in equilibrium as the ball-and-socket joint will provide the necessary resistive reactions.
 - C) The rod becomes unstable as the cables cannot support compressive forces.
 - D) The rod becomes unstable since a moment about AB cannot be restricted.





GROUP PROBLEM SOLVING



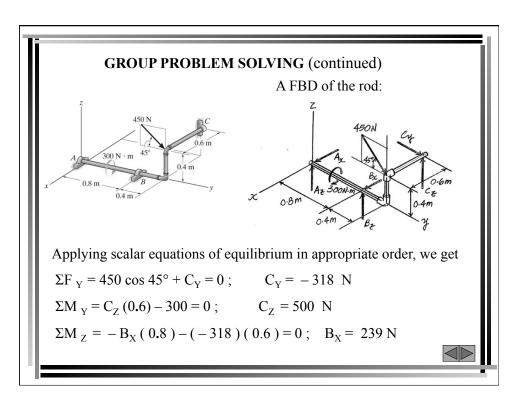
Given: A rod is supported by smooth journal bearings at A, B, and C. Assume the rod is properly aligned.

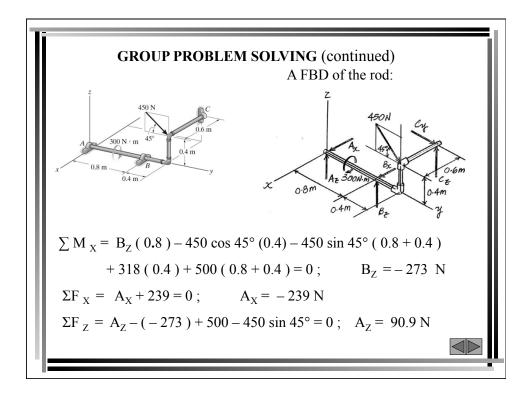
Find: The reactions at all the supports for the loading shown.

Plan:

- a) Draw a FBD of the rod.
- b) Apply scalar equations of equilibrium to solve for the unknowns.







ATTENTION QUIZ

- 1. A plate is supported by a ball-and-socket joint at A, a roller joint at B, and a cable at C. How many unknown support reactions are there in this problem?
 - A) 4 forces and 2 moments
 - B) 6 forces
 - C) 5 forces
 - D) 4 forces and 1 moment

ATTENTION QUIZ

- 2. What will be the easiest way to determine the force reaction B_Z ?
 - A) Scalar equation $\Sigma F_Z = 0$
 - B) Vector equation $\Sigma M_A = 0$
 - C) Scalar equation $\Sigma M_Z = 0$
 - D) Scalar equation $\Sigma M_Y = 0$

